

Trigonometry

$$\cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\sin(A+B) = \sin A \cos B + \sin B \cos A$$

$$\sin(A-B) = \sin A \cos B - \cos A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

$$\sin(2A) = 2 \sin A \cos A$$

$$\cos(2A) = \cos^2 A - \sin^2 A$$

$$\tan(2A) = \frac{2 \tan A}{1 - \tan^2 A} \quad \left| \begin{array}{l} \tan^{-1} \infty \\ = \frac{\pi}{2} \end{array} \right.$$

$$1 + \tan^2 A = \sec^2 A$$

$$1 + \cot^2 A = \operatorname{cosec}^2 A$$

$$R \sin(\theta + \alpha) \text{ or } R \cos(\theta + \alpha)$$

$$R = \sqrt{a^2 + b^2} \rightarrow \begin{array}{cc} 11 \sin \theta & + \quad 5\sqrt{3} \cos \theta \\ a & \quad \quad b \end{array}$$

$$\tan \alpha = \frac{\sin \alpha}{\cos \alpha}$$

$$\begin{array}{l} 1 + \cos \theta = 2 \cos^2 \left(\frac{\theta}{2} \right) \\ 1 - \cos \theta = 2 \sin^2 \left(\frac{\theta}{2} \right) \end{array}$$

Integration

$$\int e^x dx = e^x + c$$

$$\int \frac{1}{x} dx = \ln x + c$$

$$\int \frac{1}{x^2 + 1} dx = \tan^{-1}(x) + c$$

$$\int \frac{1}{x^2 + a^2} dx = \frac{1}{a} \tan^{-1} \left(\frac{x}{a} \right) + c$$

$$\int e^{ax+b} dx = \frac{e^{ax+b}}{a} + c$$

$$\int \frac{1}{(Ax+B)^2 + a^2} = \frac{1}{a} \tan^{-1} \left(\frac{Ax+B}{a} \right) \times \frac{1}{A}$$

Differentiation

$$\text{Product Rule: } \frac{d}{dx} (uv) = u'v + uv'$$

$$\text{Quotient Rule: } \frac{d}{dx} \left(\frac{u}{v} \right) = \frac{v u' - u v'}{v^2}$$

$$\frac{d}{dx} e^x = e^x$$

$$\frac{d}{dx} e^{ax+b} = a e^{ax+b}$$

$$\frac{d}{dx} \ln(x) = \frac{1}{x}$$

$$\frac{d}{dx} A \ln(ax+b) = \frac{A}{ax+b} \text{ or } \frac{f'(x)}{f(x)}$$

$$\frac{d}{dx} \sin x = \cos x \quad \left| \frac{d}{dx} \sin(ax+b) \right.$$

$$\frac{d}{dx} \cos x = -\sin x \quad \left| \begin{array}{l} \text{Area of} \\ \text{segment} \end{array} \right.$$

$$\frac{d}{dx} \tan x = \sec^2 x = \frac{1}{2} r^2 (\theta - \sin \theta)$$

$$\frac{d}{dx} \sin(ax+b) = a \cos(ax+b)$$

$$\frac{d}{dx} \cos(ax+b) = -a \sin(ax+b)$$

$$\frac{d}{dx} \tan(ax+b) = a \sec^2(ax+b)$$

$$\frac{d}{dx} \sec(ax+b) = a \sec(ax+b) \tan(ax+b)$$

$$\sin^2 x = \frac{1 - \cos 2x}{2}$$

$$\cos^2 x = \frac{1 + \cos 2x}{2}$$

$$\int \sin x dx = -\cos x + c$$

$$\int \sin(ax+b) dx = -\frac{\cos(ax+b)}{a} + c$$

$$\int \cos x dx = \sin x + c$$

$$\int \cos(ax+b) dx = \frac{\sin(ax+b)}{a} + c$$

$$\int \sec^2 x dx = \tan x + c$$

$$\int \sec^2(ax+b) = \frac{\tan(ax+b)}{a} + c$$

$$\int \frac{f'(x)}{f(x)} = \ln(f(x)) + c$$

$\Rightarrow$ Multiplication

$$u \int v = \int v du \cdot \frac{du}{dx}$$